

Capacitance of metal spheres and of a spherical

capacitor (Item No.: P2420300)

Curricular Relevance



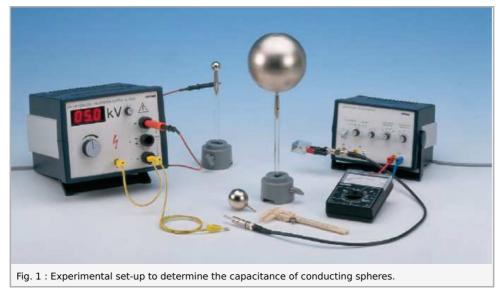
Keywords:

Voltage, potential, charge, electric field, electrostatic induction, electrostatic induction constant, capacitance, capacitors, dielectrics

Introduction

Overview

Metal spheres with different radii and a spherical capacitor are charged by means of a variable voltage. The induced charges are determined with a measuring amplifier. The corresponding capacitances are deduced from voltage and charge values.





Equipment

Position No.	Material	Order No.	Quantity
1	Conductor ball, d = 20 mm	06236-00	2
2	Conductor ball, d = 40 mm	06237-00	1
3	Conductor ball, d = 120 mm	06238-00	1
4	Hemispheres, Cavendish type	06273-00	1
5	Hollow plastics ball, w. eyelet	06245-00	1
6	Capillary tube, straight, l = 250 mm	36709-00	1
7	Copper wire, $d = 0.5 \text{ mm}$, $I = 50 \text{ m}$	06106-03	1
8	Insulating stem	06021-00	2
9	High-value resistor, 10 MOhm	07160-00	1
10	High voltage supply unit, 0-10 kV	13670-93	1
11	Capacitor/ case 1/ 10 nF	39105-14	1
12	Universal measuring amplifier	13626-93	1
13	Multi-range meter A	07028-01	1
14	Digital multimeter	07134-00	1
15	Connecting cord, 30 kV, I = 1000 mm	07367-00	1
16	Screened cable, BNC, I = 750 mm	07542-11	1
17	Adapter, BNC socket - 4 mm plug	07542-20	1
18	Connector, T type, BNC	07542-21	1
19	Adapter, BNC-plug/socket 4 mm	07542-26	1
20	Vernier caliper, plastic	03014-00	1
21	Barrel base -PASS-	02006-55	2
22	Support base -PASS-	02005-55	1
23	Right angle clamp -PASS-	02040-55	4
24	Support rod -PASS-, square, I = 630 mm	02027-55	1
25	Support rod -PASS-, square, I = 400 mm	02026-55	1
26	Universal clamp with joint	37716-00	1
27	Croco. clip, insul., strong, 10 pcs	29426-03	1
28	Connecting cord, I = 100 mm, green-yellow	07359-15	1
29	Connecting cord, I = 750 mm, green-yellow	07362-15	3
30	Connecting cord, I = 500 mm, blue	07361-04	3
31	Connecting cord, I = 500 mm, red	07361-01	3

Tasks

- 1. Determination of the capacitance of three metal spheres with different diameters.
- 2. Determination of the capacitance of a spherical capacitor.
- 3. Determination of the diameters of each test body and calculation of their capacitance values.



Set-up and procedure

Part 1

The experimental set-up to determine the capacitance of spherical conductors is shown in Fig. 1. Fig. 2 only shows the part of the experimental set-up which must be modified in order to determine the capacitance of a spherical capacitor. The spherical conductor (d = 2 cm) held on a barrel base and insulated against the latter is connected by means of the high voltage cord over the 10 M Ω - protective resistor to the positive pole of the 10 kV output of the high voltage power supply. The negative pole is earthed. This sphere is briefly brought into contact with the test spheres to charge it.

High voltage always must be reset to zero after charging. After every measurement, the charging voltage is increased by 1 kV. Before being charged anew, the test spheres must be discharged through contact with the free earth connecting cable. The charges of the test spheres are determined with a measuring amplifier. The high-resistance input of the electrometer is used for this. An auxiliary 10 nF capacitor is connected in parallel to the BNC test cord fitted with the adapter required to take over the charge. The capacitances of the spherical conductors are determined from the voltage and charge values; this is done using the average calculated over a number of charge measurement values.

Never apply high voltage to the amplifier input.

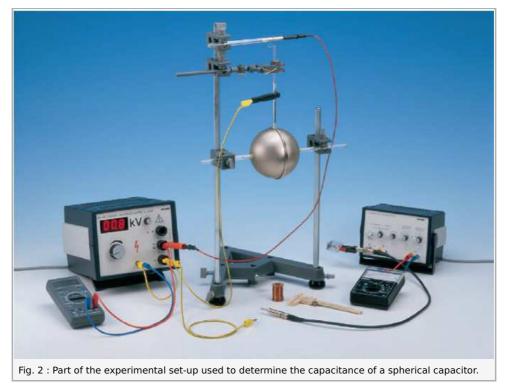
Part 2

To determine the capacitance of a spherical capacitor, the experimental set-up is altered as shown in Fig. 2. The Cavendish hemispheres are put together so as to form a complete sphere with a small circular orifice at the top. The plastic sphere with conducting surface is suspended from a copper wire in the centre of the sphere. The copper wire is lead

through a glass capillary tube which is wrapped in earthed aluminium foil to neutralise stray capacitances (Fig. 3). The aluminium foil may not touch the hemispheres.

The interior sphere must be connected to the central socket of the high voltage power supply. This is done by means of a crocodile clip over the high voltage cord, before which a 10 M Ω protective resistor is connected. The lower socket is earthed again.

Voltage is increased in steps of 100 V and may not increase above 1000 V for the safety of the digital multimeter. The corresponding mean values of the charges are read determined for the hemispheres similarly as described in Part. After every measurement, the hemispheres must be discharged with the free earthing cord. Whilst doing this, it must be assured that no high voltage is induced.



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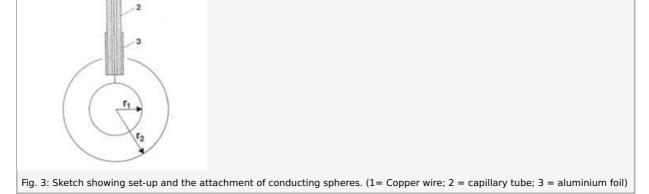
Theory and evaluation

Part 1

The capacitance C of a sphere with radius R is given by:

$$C = 4\pi \varepsilon_0 R$$

Using (1), the capacitance of the conducting spheres may be calculated: Sphere (2R₁ = 0.121 m) : $C = 6.7 \cdot 10^{-12} \text{ As/V} = 6.70 \text{ pF}$ Sphere (2R₂ = 0.041 m) : $C = 2.28 \cdot 10^{-12} \text{ As/V} = 2.28 \text{ pF}$ Sphere (2R₃ = 0.021 m) : $C = 1.22 \cdot 10^{-12} \text{ As/V} = 1.22 \text{ pF}$



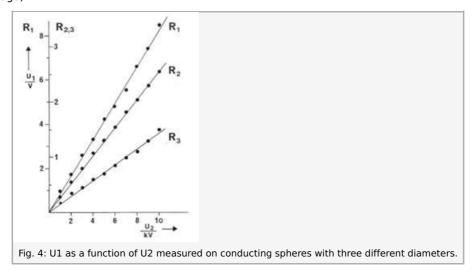
Using (2), the voltage values U_1 , which were determined by means of the measuring amplifier, allow to determine the corresponding charge value Q:

$$Q = (C_{co} + C_{ca})U_1 = (C_{co} + C_{ca})\frac{U}{V}$$
,

with

$$C_{co} << C_{ca}$$
 , $C_{ca} U_1 = rac{U}{V}$

 C_{co} = capacitance of the conductors; C_{ca} = capacitance of the parallel capacitor, U = displayed voltage, V = amplification factor, U_1 = measured voltage)



On the other hand, the charge Q of the conductor is:



(1)

(2)

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 $Q = C_{co}U_2$

Finally, charges may be calculated using (2) and (3).

$$U_1/U_2 = C_{co}/C_{ca}$$

Fig. 4 shows charging voltage values U_2 as a function of measurement voltage U_1 for the different conducting spheres. With the slope of the lines and knowing C_{ca} , the capacitances of the conducting spheres are obtained:

$$C(R_1)$$
 = 7.55 pF; $C(R_2)$ = 2.33 pF; $C(R_3)$ = 1.32 pF

(With the assistance of a measuring bridge, the capacitance C_{ca} of the parallel capacitor was determined separately to be C_{ca} = 9.1 nF. If exact capacitance determination is impossible, the nominal capacitance value of the capacitor must be used for calculation; this may, however, be affected by design tolerance deviations of \pm 10%).

Part 2

The capacitance C of a spherical capacitor is given by

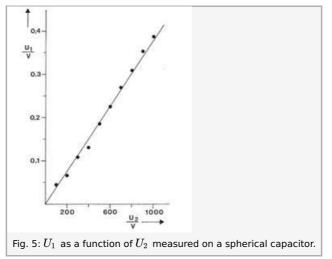
$$C = 4\pi\varepsilon_0(\frac{r_1r_2}{r_2 - r_1} \tag{4})$$

(r_1 = Radius of the interior sphere; r_2 = Radius of the exterior sphere)

With r_1 = 0.019 m and r_2 = 0.062 m for the spherical capacitors, capacitance calculation yields C = 3.0 pF. Fig. 5 once more represents measurement value pairs U_1 and U_2 .

According to the assessment procedure described above and using the slope of the graph line, the empirically determined capacitance of the spherical capacitor is found to be C = 3.5 pF.

Capacitance values determined experimentally are always higher than the calculated values. This discrepancy is due to unavoidable dispersive capacitances.





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